

# Electromagnetic field analysis of novel low cogging force, linear switched reluctance motor, based on 2-D finite element method

## Authors

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## ABSTRACT

*This paper deals with electromagnetic design and 2-D (two-dimensional) magnetic field analysis of novel low force ripple linear switched reluctance (LSR) motor. The configuration that has been presented here has a higher number of rotor poles than stator poles, and the purpose of this configuration is to improve the force ripple, which is the weak point of LSRMs. In order to illustrate the conformity of the design parameter's stage in this study, the calculated values of the magnetic field and cogging force characteristics are compared with that of their desired values. Also, the proposed configuration is compared to a 6-4 and 3-phase conventional LSRM with similar number of stator teeth, number of phases, and constraints in volume. From the numerical analysis of a proposed novel configuration, it has been observed that this machine produces higher force per unit volume and almost similar cogging force when compared to a conventional LSRM with identical number of stator teeth, number of phases, and constraints in volume. The obtained primary electric and magnetic characteristics for the proposed configuration are verified with the help of 2-D FE computations.*

## Article history:

Received : 21 April 2017

Accepted : 13 June 2017

**Keywords:** FE Computation, Magnetic Field analysis, 2-D FEM, SR Motor.

## 1. Introduction

Linear Switched reluctance motors (LSRMs) are attractive due to their simple structure, low cost in mass production, high performance and efficiency, lesser maintenance requirement, fault tolerance, rugged motor construction, high force over a wide speed range, and easy speed control [1–4]. Hence, due to these advantages, during the past few decades LSRM has been the focus of intensive research efforts for variable speed application in industries [5, 6]. However, it

has an inherent high cogging force due to its salient structure, which results in an undesirable acoustic noise and mechanical vibration. In order to apply LSRM and SRM to the industrial field, the force ripple has to be reduced [7, 8]. Rotary SRM torque ripple reductions have been investigated in many studies using two main approaches, the geometric design parameter change and electronic control strategies. The geometric design approach is based on optimizing the salient pole shapes, especially salient pole arc, such as stator pole arc ( $\beta_s$ ) and rotor pole arc ( $\beta_r$ ) [9–11]. The electronic control strategy is based on the selection of an

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optimum combination of electric design parameters, such as turn on and turn off angles ( $\theta_{on}$  and  $\theta_{off}$ ), level of current, and supply voltage [12–15]. A novel stator pole shape with non-uniform air-gap and a pole shoe on rotor pole to reduce the torque ripple was investigated in [16, 17]. A new hybrid stator-pole that improves the radial force is described in [18]. This paper presents electromagnetic design and magnetic field analysis, and predicts the electromagnetic behavior of a novel configuration linear switched reluctance motor, which has a higher number of rotor poles than stator poles. The purpose of this configuration is to improve cogging force. To predict the electromagnetic behavior and estimate the overall performance of the proposed novel configuration, 2-D finite element method has been utilized.

Numerical techniques, such as FE computation, can be utilized for modeling and predicting the electromagnetic behavior, especially in novel configurations studies for different operation modes. The electromagnetic characteristics, such as inductance, terminal induced Back-EMF, precise flux linkage, and mutual inductance, can be obtained by magnetic field computation inside the machine. FE method utilizes materials property, machine geometry, and all the boundary conditions for magnetic field computation.

Numerical techniques, such as Finite Element Method (FEM), is suggested by different researchers for modeling and parameter identification of electrical machines [19–25]. In a reference [26], a novel topology of tubular motor with a modular construction and high specific thrust that can be used for various applications has been presented. Again, in another reference [27], an electromagnetic design and 3-D magnetic field analysis of a novel configuration machine based on a hybrid analytical, assisted by BLDC field and 3-D FEM analysis has been presented. In this paper, the design methodology obtained primary magnetic and electric characteristics for the configuration under study and is verified by 3-D FE computation. The design and analysis of a two double-rotor flux-modulated permanent-magnet machine for direct-drive applications by using the time-stepping finite element method has been presented in a reference [28]. A reference [29] showed the development of MGs. Hence, in this study, the MGPM machines have been presented and discussed, with emphasis on providing

performance analysis and a quantitative comparison of three viable MGPM machines. A novel double-winding flux-modulated permanent magnet machine (FMPM) for stand-alone wind power generation is presented in reference 30. The results showed that the proposed FMPM has a higher torque capability and stronger flux adjustability than the existing single-winding FMPMs. In reference 31, a novel dual Halbach array has been proposed to enhance flux density in the air gap, thus improving the output performance of linear machines. In this paper, the numerical results from finite element method are employed to simulate and observe the flux distribution in the machine. In a reference [32], the design and analysis of an inside-out axial-flux permanent magnet (AFPM) synchronous machine optimized by genetic algorithm (GA) based sizing equation, finite element analysis (FEA), and finite volume analysis (FVA) has been demonstrated. The modeling of the brushed DC motor used as a reinforced starter for a micro-hybrid automotive application has been presented in reference 33. The design criteria for a tubular linear induction motor (TLIM) as fast actuators has been shown in reference 34. The influence of geometrical and physical parameters on the operating conditions of a TLIM are investigated by the means of a quasi-analytic model.

This paper is organized as follows: The introduction is presented in Section I. Section II of the paper focuses on the principle operation of the proposed novel structure. Dynamic mathematical model is presented in section III. The sections thereafter describe different ways of obtaining the flux-linkage characteristics for SRM and LSRM. Section V describes design calculations of the proposed 6/10 three-phase LSRM. The subsequent sections describe numerical analysis and discussion on magnetic field for the proposed SR machine. The detailed simulation and magnetic optimization are presented in section VII. The conclusion is presented at the end.

## 2. Principle operation of proposed novel structure

The principle operation of LSRM is similar to the rotary switched reluctance motor (RSRM). It should be noted that the LSRM produces linear force and RSRM produces rotational torque. It can be assumed that LSRM is merely a ‘rolled out’ version of a RSRM. In LSRM, the translator (or rotor) is the moving

part and the stator is the stationary part in which linear force production occurs due to the tendency of the translator to move towards a separate stationary point where the inductance of the excited winding is maximum. During the past few decades, several configurations for the LSRM, including various combinations of rotor and stator poles, have been studied [1]. Some well-known configurations of regular stator and rotor poles are given as Table 1.

The proposed configuration in this paper is an LSRM with more rotor poles than stator poles.

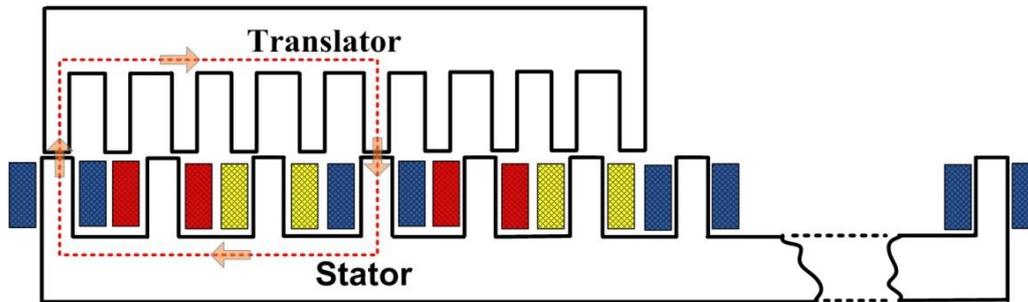
This LSRM consist of salient pole in both of stator, with six salient poles ( $N_s$ ) and translator, with ten salient poles ( $N_r$ ). In the proposed configuration, the number of

turns in each phase has been increased because of the availability of more slot area. Hence, it was possible to increase the overall force per unit volume. In this configuration, both the stator and translator consist of stacked laminations. The stator consists of stacked laminations with concentrated winding wrapped around the salient poles. Figure 1 shows the complete assembly of the proposed 6-10 machine with phase winding. Figure 2 shows the complete assembly of the conventional 6-4 machine with phase winding.

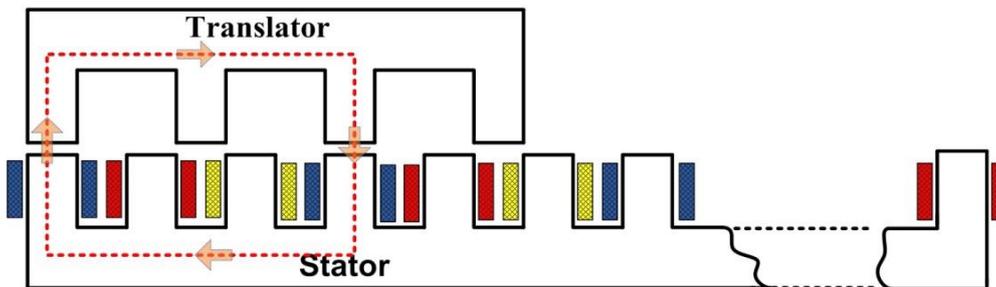
Understudy conventional LSRM is a 3-Phases and 6-4 configuration, consist of salient pole in both of stator, with six salient poles ( $N_s$ ) and translator, with four salient poles ( $N_r$ ).

**Table 1.** Several LSRM configurations with regular stator and rotor poles.

Phase Number		$N_s/N_r$						
1	Three-Phase	6/2	6/4	6/8	6/14	12/8	18/12	24/16
2	Four-Phase	8/6	8/10	16/12	24/18	32/24		
3	Five-Phase	10/4	10/6	10/8	10/12			
4	Six-Phase	12/10	12/14	24/20				
5	Seven-Phase	14/10	14/12	14/16				



**Fig. 1.** Complete assembly of proposed 6-10 LSRM with phase winding



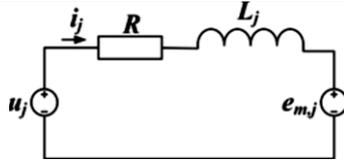
**Fig. 2.** Complete assembly of proposed 6-4 LSRM with phase winding

### 3. Dynamic mathematical model

Mathematical equations of the electric circuit for each phase, and mechanical part of the LSRM are the basis of the dynamic model [35, 36]. Flux-linkage characteristics and its derivatives are required for simulation of

the LSRM, based on the dynamic mathematical model. Special attention should be paid to its determination to ensure reliability of the obtained model. The mathematical equations and dynamic model of SRM and LSRM per phase are given as Table 2.

**Table 2.** The mathematical equations and Dynamic Model of SRM and LSRM Per Phase  
The Mathematical Equations Of The Electric Circuit



Electrical Equivalent Circuit Per Phase of an LSRM

The Voltage  
Phase Equation:

$$u_j = \frac{\partial \psi_j(x, i_j)}{\partial t} + R i_j$$

$$= \frac{\partial \psi_j(x, i_j)}{\frac{\partial i}{L_j}} \frac{d i_j}{dt} + R i_j$$

$$+ \frac{\partial \psi_j(x, i_j)}{\frac{\partial x}{e_{m,j}}} v$$

Instantaneous  
Electromagnetic  
Force ( $F_e$ ) Per  
Phase

$$u_j = L_j \frac{d i_j}{dt} + e_{m,j} + R i_j$$

$$F_e = \sum_{j=1}^m \left( \frac{\partial}{\partial x} \left( \int_0^i \psi_j(x, i_j) d i_j \right) \right)_{I=ctn}$$

$$F_e = M \frac{d v}{dt} + F_r + F_L$$

$$v = \frac{1}{M} \int (F_e - F_r - F_L) \cdot dt$$

$$\frac{d i_j}{dt} = \left( \frac{\partial \psi_j(x, i_j)}{\partial i_j} \right)^{-1} \left( u_j - R i_j - \frac{\partial \psi_j(x, i_j)}{\partial x} v \right)$$

Dynamic Model  
of LSRM Per  
Phase

$$\frac{d v}{dt} = \frac{1}{M} (F_e - F_r - F_L)$$

$$i_j = \int \left( \frac{\partial \psi_j(x, i_j)}{\partial i_j} \right)^{-1} \cdot \left( u_j - R i_j - \frac{\partial \psi_j(x, i_j)}{\partial x} v \right) dt$$

$$\frac{d i_j}{dt} = \frac{1}{\frac{d^2 W_{co}(i_j, \alpha)}{d i^2}} \left( u_j - R i_j - \frac{d^2 W_{co}(i_j, \alpha)}{d i_j d \alpha} \omega \right)$$

Dynamic Model  
of Rotary SRM  
Per Phase

$$T_e(i, \alpha) = \frac{d W_{co}(i_j, \alpha)}{d \alpha} = J \frac{d^2 \alpha}{dt^2} + B \frac{d \alpha}{dt} + T_l$$

$$W_{co}(i_j, \alpha) = \int_0^i \lambda(i_j, \alpha) d i$$

$R$ : Phase resistance

$L_j$ : Inductance

$\psi_j$ : Flux linkage

$u_j$ : Applied voltage

$F_e$ : Electromechanical force produced

$F_L$ : Mechanical load

$F_r$ : Friction

$M$ : Translator mass

$v$ : Velocity

$x$ : Position

$\alpha$ : The rotor position.

$\omega$ : The angular velocity.

$W_{co}$ : The co – energy.

$T_e$ : The instantaneous electromagnetic

$T_l$ : The load torque.

$J$ : The moment of inertia.

$B$ : The coefficient of friction

**4. The different was of obtaining flux-linkage characteristics for SRM and LSR**

Table 3 presents the three different ways of obtaining flux-linkage characteristics or magnetization curves, two of them are based on FEA and the last one on experimental measurements, which validate previous finite element (FE) methodologies.

**5.Design calculation of proposed 6/10 three-phase LSRM**

The proposed design procedure utilizes the rotating switched reluctance machine design by converting the specifications of the linear machine into those of an equivalent rotating machine. The machine design is carried out in the rotary section, which is then transformed back into the linear section. The proposed configuration is designed with the following specifications (Table 4).

The acceleration (maximum acceleration if  $t_a = t_d$ ) is:

$$a_a = \frac{v_m}{t_a} \tag{1}$$

The force for initial acceleration is calculated as:

$$a_g = 9.8 \text{ m/s}^2 \tag{2}$$

$$F_a = M_t \cdot (a_a + a_g) \tag{3}$$

if deceleration  $a_d = -0.6 \text{ m/s}^2$ .

Instantaneous deceleration force is given as:

$$F_a = M_t \cdot (a_a + a_g) \tag{4}$$

Maximum power capacity of the LSRM (if  $f_f=0$ ) as:

$$\begin{cases} P = F_a \cdot v_m \\ P = k_e k_d k_1 k_2 B_g A_{sp} D^2 L N_r \\ L = KD \\ P = k_e k_d k_1 k_2 B_g A_{sp} D^2 v_m \frac{60}{\pi} \end{cases} \tag{5}$$

**Table 3.**Three different ways of obtaining flux-linkage characteristics

Different Ways of Obtaining Flux-Linkage Characteristics	
2D FE Model	$\psi_{2D} = N_{PP} N \oint_C \bar{A} d\bar{l}$ $\begin{cases} \text{Range of position } x & \begin{cases} \Delta s \Rightarrow \{x=0 \text{ (Fully unaligned)} \\ x=s \text{ (Full aligned)} \end{cases} \\ \text{Density Current } J & \begin{cases} \Delta j \Rightarrow 0 \text{ to } 15 \text{ A/mm}^2 \end{cases} \end{cases}$ $\begin{cases} \text{Range of position } x & \begin{cases} \Rightarrow \{x=0 \text{ (Fully unaligned)} \\ x=s \text{ (Full aligned)} \end{cases} \\ \text{Density Current } J & \begin{cases} \Delta j \Rightarrow 0 \text{ to } 20 \text{ A/mm}^2 \end{cases} \end{cases}$
3D FE Model	$\psi_{3D}(x, i) = \frac{N_{PP} N}{i} \iiint \bar{A} \bar{J} dV$ <p><math>N_{PP}</math> Pole-Coil, N Turn per coil, The current is obtained by:</p> $i = \iint_s \bar{J} \cdot d\bar{s}$
Experimental measurements	Experimental measurements validate previous finite element (FE) methodologies.

**Table 4.** Specifications of Proposed LSRM

$L_t$	Stator Length of LSRM	1 m
$V_m$	Maximum Linear Velocity	0.9 m/sec
$t_a$	Acceleration Time	1.5 sec
$M_t$	Maximum Mass of Translator Assembly	35 kg
$t_d$	Deceleration	- 0.6 m/sec <sup>2</sup>

The bore diameter is obtained from the power output equation:

$$D = \sqrt{\frac{P\pi}{60k_e k_d k_1 k_2 B_g A_{sp} v_m}} \quad (6)$$

$$C_{sy} = \frac{D\beta_s}{2} \quad (7)$$

$$h_s = \frac{D_0}{2} - \frac{D}{2} - C_{sy} \quad (8)$$

$$C_{ry} = \frac{D\beta_r}{2} \quad (9)$$

$$h_r = \frac{D}{2} - g - C_{ry} \quad (10)$$

$$\phi = B_g A_g \quad (11)$$

$$A_g = \left(\frac{D}{2} - g\right) \left(\frac{\beta_r + \beta_s}{2}\right) L \quad (12)$$

$$H_g = \frac{B_g}{\mu_0} \quad (13)$$

Ampere-turns required producing the air gap magnetic field intensity

$$\begin{cases} T_{ph} I_p = H_g \cdot 2g \\ T_{ph} = \frac{H_g \cdot 2g}{I_p} \\ a_c = \frac{I_p}{J\sqrt{m}} \end{cases} \quad (14)$$

$$W_{sp} = C_{ry} \quad (15)$$

$$W_{tp} = C_{sy} \quad (16)$$

where  $A_g$ : cross-section area of the air gap,  $W_{sp}$ : stator pole width,  $W_{ss}$ : stator slot width,  $W_{tp}$ : translator pole width,  $W_{ts}$ : translator slot width,  $C_{sy}$ : stator yoke

thickness,  $h_s$ : height of the stator pole,  $C_{ry}$ : translator yoke thickness,  $H_g$ : magnetic field intensity,  $J$ : current density,  $T_{ph}$ : number of winding turns per phase,  $I_p$ : phase current,  $a_c$ : conductor area,  $m$ : phase number,  $\phi$ : motor flux linkage,  $\beta_s$ : stator pole angle,  $\beta_r$ : translator pole angle,  $k_e$ : efficiency,  $k_d$ : duty cycle,  $k_1 = \frac{\pi^2}{120}$ ,  $k_2$ : a variable dependent on aligned saturated inductance and unaligned inductance,  $B_g$ : air gap flux density,  $A_{sp}$ : specific electric loading,  $D$ : bore diameter,  $L$ : stack length, and  $N_r$ : rotor speed. The dimensions of the designed three phases LSRM is shown in Fig.3.

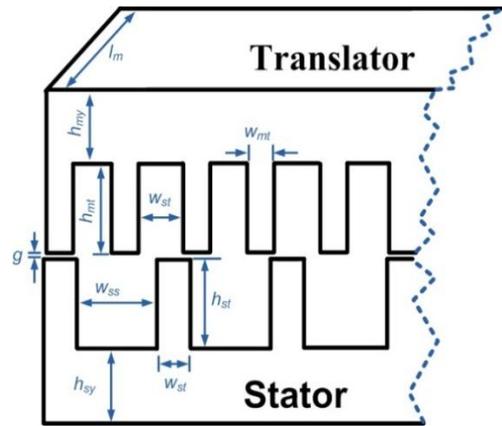


Fig. 3. Dimensions of the designed three-phase LSRM

The calculated design parameters of the proposed 6-10 and conventional 6-4 LSRM are summarized as follow (Table 5).

Table 5. Design specifications of both the motors

Items	6-10 LSRM	6-4 LSRM
Translator width, $l_m$ (mm)	60	60
Translator tooth width, $w_{mt}$ (mm)	19	30
Translator slot width, $w_{st}$ (mm)	21	54
Translator tooth high, $h_{mt}$ (mm)	25	25
Translator yoke high, $h_{my}$ (mm)	20	20
Stator tooth width, $w_{st}$ (mm)	20	28
Stator slot width, $w_{ss}$ (mm)	55	28
Stator tooth high, $h_{st}$ (mm)	30	30
Stator yoke high, $h_{sy}$ (mm)	23	23
Air gap length, $g$ (mm)	0.8	0.8
Number of turns per coil, $N_{coil}$	220	198
Rate current, $I_{RMS}$ (A)	11	14

**6. Numerical analysis of magnetic field for the proposed SR machine**

For an accurate calculation of the magnetic field distribution, prediction of the characteristics of machine magnetization and design validation of the proposed machine with the help of complex geometry and nonlinear properties, and numerical technique must be carried out. As mentioned in section IV, FEM is one of the most popular numerical calculation techniques for electromagnetic fields, which have been widely developed for magnetic analysis of electrical machines. In this paper, 2-D FEM is utilized for the calculation and analysis of electromagnetic fields, in and around the proposed configuration. Precise information and electromagnetic characteristics obtained from FE computation is utilized to confirm and describe the principle operation and magnetic behavior of the proposed novel configuration. In this study,  $T - \Omega$  formulation, which is a common method for solving magnetic field problems, has been utilized for electromagnetic field solution. In  $T - \Omega$  formulation,  $T$  defined as [37, 38]:

$$j = \nabla \times T \tag{17}$$

From Maxwell's equation we have:

$$j = \nabla \times T = \nabla \times H \tag{18}$$

Then:

$$\nabla \times (H - T) = 0 \tag{19}$$

Since the vector  $H - T$  can be expressed as the gradient of a scalar, i.e.

$$H = T - \nabla\Omega \tag{20}$$

where  $\Omega$  is a magnetic scalar potential. Also, since

$$\nabla \times E = -\frac{\partial B}{\partial t} \tag{21}$$

Then,

$$\begin{aligned} \nabla \times E &= \nabla \times \left[ \left( \frac{1}{\sigma} \right) \nabla \times T \right] \\ &= -\frac{\partial B}{\partial t} = \mu_0 \mu_r \left( \frac{\partial}{\partial t} \right) (T - \nabla\Omega) \\ &= -\mu_0 \mu_r \left( \frac{\partial T}{\partial t} \right) - \nabla \left( \frac{\partial \Omega}{\partial t} \right) \end{aligned} \tag{22}$$

which finally reduces to the following two scalar equations[19, 20]:

$$\nabla^2 T - \mu\sigma \left( \frac{\partial T}{\partial t} \right) = -\mu\sigma \nabla \left( \frac{\partial \Omega}{\partial t} \right) \tag{23}$$

and

$$\nabla^2 \Omega = 0 \tag{24}$$

Due to the complex geometry, nonlinear property, and magnetic saturation effect, the design procedure and evaluation of accuracy of the proposed novel configuration became more complicated. It must be noted that for proper operation, the proposed configuration was expected to work under full saturation condition.

**7. Simulation and magnetic optimization**

To confirm the design procedure of the proposed LSRM and the precision of the analytical model, 2-D FE analysis is used. The inductances and flux linkages of the phase windings, normal forces, and propulsion developed by the proposed configuration are determined for various excitation currents and translator positions. It should be noted that FEA, in general, provides more accurate results than the magnetic analytical method with an equivalent circuit method because it considers a large number of flux paths as compared to the magnetic equivalent circuit method.

An accurate calculation of the magnetic field distribution is obtained using the Magnet CAD package (Infolytica Corporation Ltd). In order to obtain precise information about electromagnetic characteristics and magnetic behavior, such as inductance, propulsion force, and normal force for different positions, the proposed LSRM translator is shifted from an unaligned position, with respect to the stator, to an aligned position. This is done at different excitation currents and the normal force, inductance, and propulsion forces, corresponding to each translator position, are obtained.

- Magnetic optimization design methodology

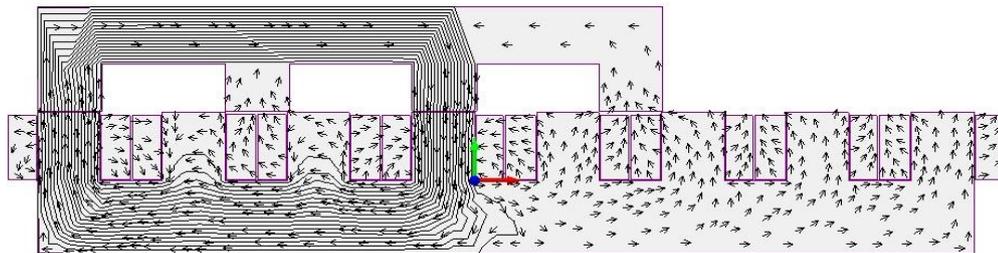
An FEM analysis optimization routine for the optimum design of a proposed 6-10 LSRM for long stator applications has been set up, which includes two FE analyses procedure. The first one is an EM FE analysis for the translator and stator pole geometry to find the minimum force ripple at different aligned to unaligned positions. The second procedure involves EM FEA for the translator at a specified position to find the minimum translator weight and electromagnetic FEA. The design

optimization searches were implemented in a commercial Magnet CAD package (Infolytica Corporation Ltd., 2007).

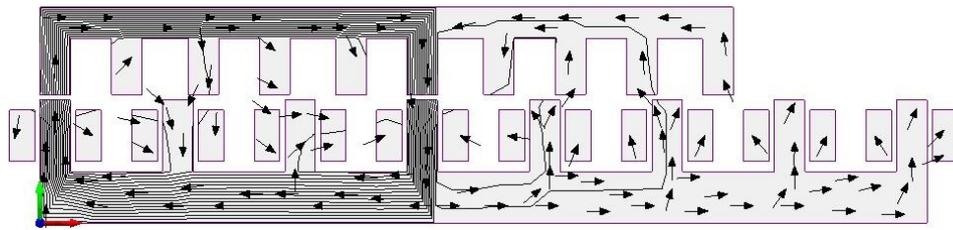
The dimensional variables were: stator and translator tooth width and tooth height, which ranged between  $h_{mt} = [22 - 27]$  mm,  $h_{st} = [28 - 32]$  mm,  $W_{mt} = [14 - 24]$  mm, and  $W_{st} = [W_{mt} \pm 0 - 2]$  mm, mover yoke thickness, and translator width. The rms current densities at low and high speeds were also set as variables. Airgap was fixed as 0.8 mm. The constraints were: maximum translator width

( $\leq 80$  mm) and maximum axial translator length ( $\leq 500$  mm). The objective was to maximize the average output force. The optimization was done for 6-10 LSRM.

Figure 4 shows the flux distributions inside the proposed 6-10 and conventional 6-4 LSRM for the fully aligned, half aligned, and unaligned positions with a phase current of 10A in one phase winding. It is observed that the leakage flux lines cross the stator slot air gap to the adjacent stator poles and complete their path through the stator back-irons.

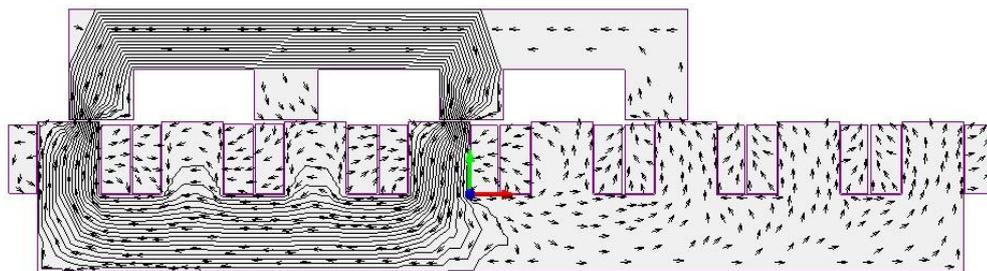


6-4 Configuration

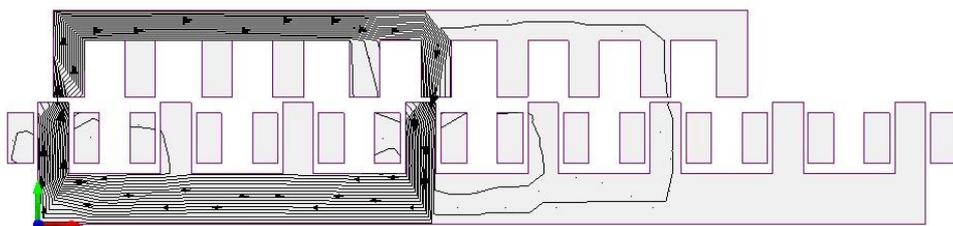


6-10 Configuration

(a) Fully aligned position



6-4 Configuration



6-10 Configuration

(b) Half aligned position

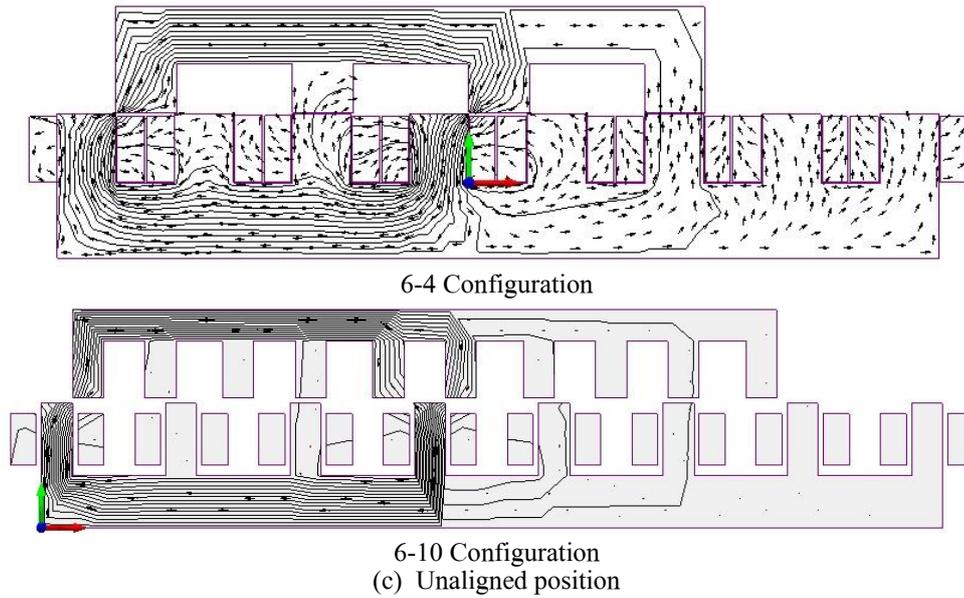


Fig. 4. Flux distribution of the 3-Phase proposed 6-10 and conventional 6-4 LSRM at rated current, 10A for (a) fully aligned, (b) half aligned and (c) unaligned position

Figure 5 shows the inductance profile obtained from FEM and analytical results at 10 A phase current for various translator positions for both conventional 6-4 and proposed novel 6-10 LSRM configuration.

Figure 6 shows the flux linkage curve from analytical and FEM analysis with three different phase currents for various translator positions. A comparison of the FEA results and analytical analysis for flux linkage versus

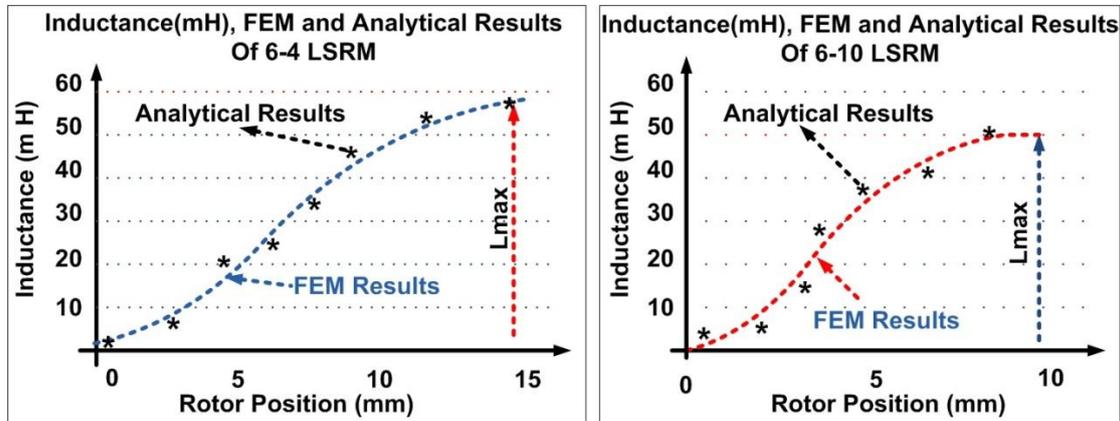


Fig. 5. Inductance curve for 6-4 and 6-10 LSRM configuration FEA and Analytical simulation results of inductance at 10A, phase current

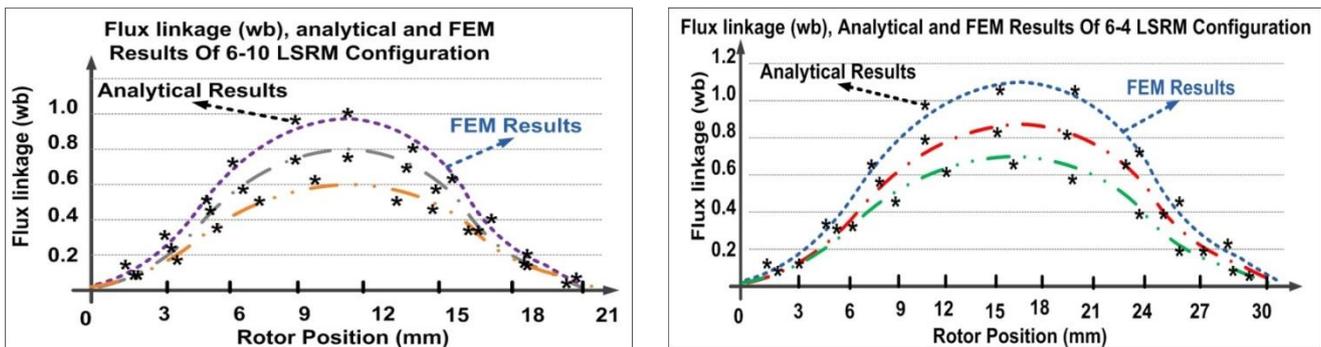


Fig. 6. FEM and Analytical Result of the flux linkage profile at several different phase currents with respect to various translator positions, 6-4 conventional and 6-10 proposed LSRM

current at various rotor positions in the 6-10 configuration LSRM is shown in Fig.7.

Figure 8 shows the propulsion force profile at different positions obtained from FEM analysis for both conventional 6-4 and the proposed 6-10 LSRM.

The obtained propulsion force profile from FEM analysis at different positions for the proposed 6-10 and conventional 6-4 LSRM are shown in Fig.8.

Figure 9 shows the obtained propulsion force profile from FEM analysis with three

different phase currents for various translator positions for the proposed 6-10 LSRM.

Figures 10 and 11 show the output force for both 6-4 conventional and 6-10 proposed LSRM. It can be observed that the 6/10 proposed LSRM shows better output torque capabilities. From Table 6 it can be observed that the 6/10 proposed LSRM produces 28% – 40% higher peak force. Also, from Table 7, it can be observed that the 6/10 proposed LSRM produces 35% – 47% higher average force.

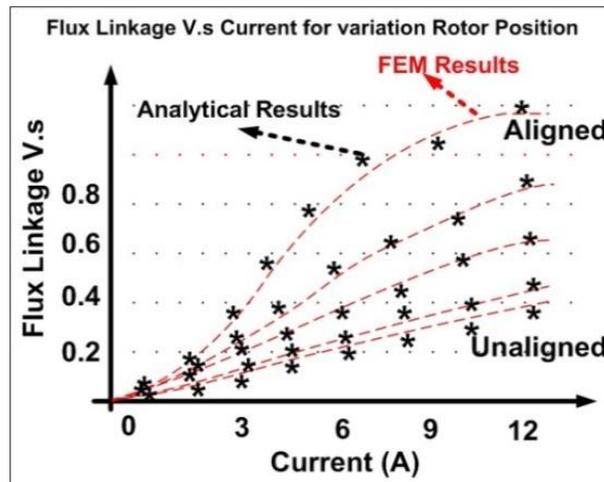


Fig.7. Flux linkage V.s Current for variation rotor position for 6-10 configuration LSRM, FEM and Analytical results

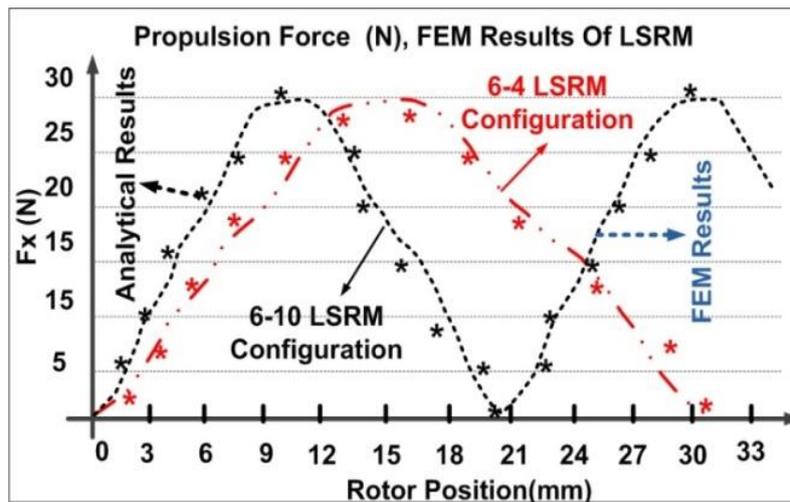


Fig. 8. analytical and FEA simulation results of propulsion force at different position

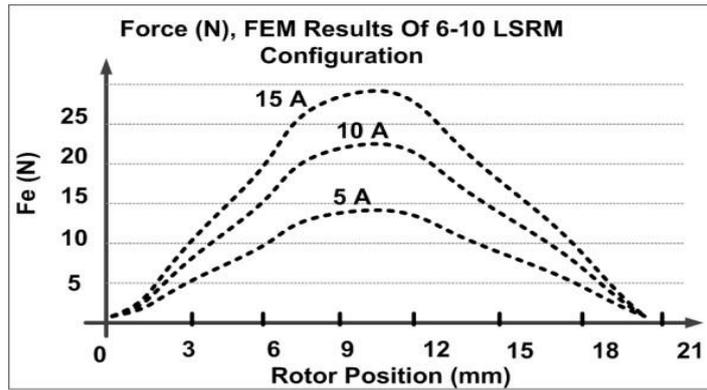


Fig. 9. FEA simulation results of propulsion force at different phase currents for 6-10 LSRM

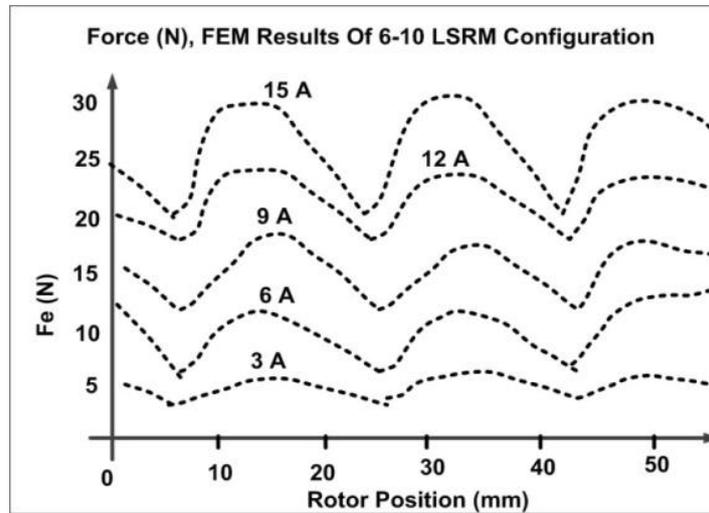


Fig. 10. FEA simulation results of propulsion force at different phase currents for 6-10 LSRM

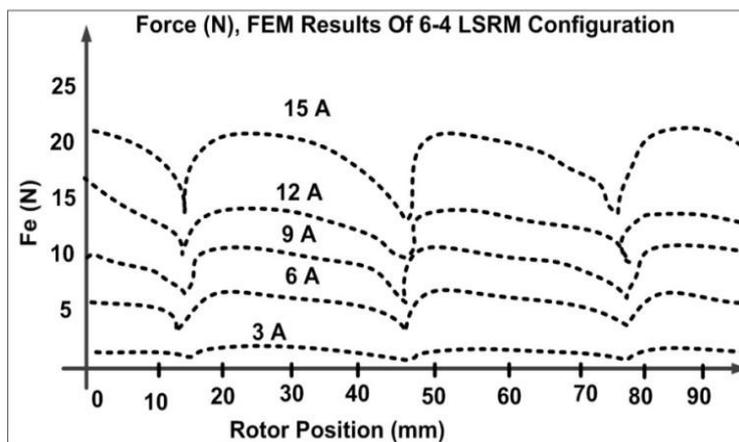


Fig. 11. FEA simulation results of propulsion force at different phase currents for 6-4 LSRM

Table 6. Peak force comparison

PEAKE FORCE COMPARISON				
Factor	Phase Current (A)	6-4 LSRM	6-10 LSRM	% Different
Peake Force	3	2.5	3.2	28
	6	5.8	8.1	39
	9	12.1	16.3	40
	12	13.8	20	39
	15	20	27	35

Table 7. Average force comparison

AVERAGE FORCE COMPARISON				
Factor	Phase Current (A)	6-4 LSRM	6-10 LSRM	% Different
Average Force	3	2	2.7	35
	6	5.2	7.6	46
	9	11.6	15.8	36
	12	13.2	19.4	47
	15	19	26.4	38

Force ripple is defined from the instantaneous force  $F_i$  as the difference between the maximum and minimum forces, expressed as a percentage of the average force. This can be written as:

$$\text{Force Ripple} = \frac{\text{Max}(F_i) - \text{Min}(F_i)}{F_{ave}} \times 100\%$$

From Table 8, it can be observed that the 6/10 proposed LSRM produces -5.5% – 33.4% lower force ripple. Finally, Table 9 shows the comparison of geometric parameters.

## 8. Conclusion

This study deals with the designing and 2-D FE computations of the magnetic field distribution for a novel configuration linear switched reluctance (LSR) motor. Comparison of the calculated magnetic field and torque characteristics with their desired values illustrate the conformity of the design parameter's stage. It has been observed

through numerical analysis that the proposed configuration gives higher force and drastically reduced force ripple. From numerical analysis of the presented configuration, it has been observed that the proposed linear motor produces higher force per unit volume and similar force ripple when compared to a conventional 6-4 LSRM with almost identical number of stator tooth, number of phases, and constraints in volume.

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Table 8. Force ripple comparison

Force Ripple Comparison				
Factor	Phase Current (A)	6-4 LSRM	6-10 LSRM	% Different
Force Ripple	3	25	18	28
	6	34	33	2.9
	9	18	19	-5.5
	12	13.6	10	26.4
	15	27	18	33.4

Table 9. Comparison of geometric parameters

Comparison of Geometric Parameters			
Parameters of Comparison	6-4 LSRM	6-10 LSRM	% Different
Cross sectional Area of Stator Tooth (mm <sup>2</sup> )	1680	1200	28
Cross sectional Area of Rotor Tooth (mm <sup>2</sup> )	1800	304	83
Cross sectional Area of Stator slot (mm <sup>2</sup> )	1680	3300	96.4

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